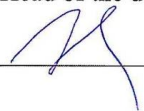


RUSSIAN MINISTRY OF SCIENCE AND EDUCATION
FEDERAL STATE BUDGETARY EDUCATIONAL INSTITUTION
OF HIGHER EDUCATION
«BASHKIR STATE UNIVERSITY»

FACULTY OF MATHEMATICS AND INFORMATION TECHNOLOGIES

Approved: at the department meeting
Protocol # 6 from January 26, 2021
Head of the department


_____ Kh.K. Ishkin

Coordinated with:
EMC chairman of the faculty/institute


_____ A.M. Efimov

WORKING PROGRAM OF DISCIPLINE (MODULE)

Discipline Analysis I

(name of the discipline)

_____ Obligatory part

(name of the part enclosing the discipline (obligatory, formed by participants of the educational activity, facultative))

bachelor (undergraduate) program

Course of training (speciality)

_____ 01.03.02 Applied mathematics and informatics

(code and name of the course of training (speciality))

Subdivision of the course of training (profile)

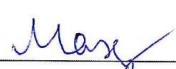

_____ Applied programming and data analysis

(name of the profile of training)

Qualification (level of training)

_____ bachelor

(name of the level of training)

Designer (compiler): associate professor of the MA department, PhD	 _____ A.A. Makhota ,
	 _____ N.F. Abuzyarova

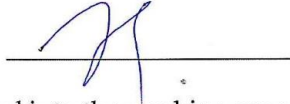
For enrollment of: 2021

Ufa 2021

Designer: associate professor, PhD Alla Aleksandrovna Makhota. associate professor,
PhD Natalia Fairbahovna Abuzyarova

The working program of the discipline is approved at the meeting of the department of
Mathematical Analysis,
protocol # 6 from January , « 26 » 2021.

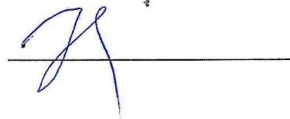
Head of the department



Kh.K. Ishkin

The addenda and updates introduced into the working program of the discipline are approved
at the meeting of the department of Higher algebra and geometry,
protocol # 11 from June , « 10 » 2021.

Head of the department



Kh.K. Ishkin

List of documents and proceedings

1. The list of planned learning outcomes of the discipline, correlated with the planned results of the educational program	4
2. The purpose and place of the discipline in the structure of the Educational Program (EP)	4
3. The content of the work program (the scope of the discipline, types and types of classes, educational and methodological support for students' independent work)	5
4. The fund of assessment tools for the discipline	
4.1. The list of competencies and indicators of achievement of competencies with an indication of the planned learning outcomes of the discipline correlated with them. Description of criteria and scales of assessment of learning outcomes in the discipline	5
4.2. Model control tasks or other materials necessary to assess the learning outcomes of the discipline, correlated with the established in the educational program indicators of achievement of competencies. Methodological materials defining the assessment procedures results of education on the discipline	8
5. Educational-methodical and informational support of the discipline	
5.1. List of basic and additional academic literature, which is necessary for mastering the discipline	15
5.2. List of resources of information and telecommunications network "Internet" and software necessary for mastering the discipline, including professional databases and information help systems	16
6. The material and technical base necessary for the implementation the educational process for the discipline	16
Appendix 1 Content of the working program	17
Appendix 2 An example of examination tickets	25
Appendix 3 Rating – plan of the discipline	26

1. The list of planned learning outcomes of the discipline, correlated with the planned results of the educational program

Mastering the discipline must lead to forming of the following competence (GPC-1):

Category (group) of competencies (if there is exist a GPC)	Competence to be formed (with the code)	Code and name of the indicator of competence achievement	Learning outcomes for the discipline
<i>Theoretical and practical basics of professional activity</i>	<i>GPC-1. Able to apply the fundamental knowledge obtained in the mathematical and/or natural sciences and use them in professional activities</i>	<i>GPC-1.1. Possesses basic knowledge obtained in the field of mathematical analysis.</i>	<i>Know the basic concepts of disciplines, basic theorems and consequences, methods of solution and analysis of typical problems</i>
		<i>GPC-1.2. Is able to use them in professional activities.</i>	<i>Be able to use in practice the knowledge of disciplines, correctly formulate tasks and reasonably choose methods of their solutions</i>
		<i>GPC-1.3. Has the skills to choose the methods of solving the problems of professional based on theoretical knowledge.</i>	<i>Master the basic mathematical knowledge and its application to the solution of problems theoretical and applied character</i>

2. The discipline "Mathematical Analysis" is part of the basic part. The discipline is studied at the 1.2 courses in semesters 1-3.

The purpose of the discipline: studying the basics of mathematical analysis, combining the theory of real numbers, the theory of limits, the theory of series, differential and integral calculus and their direct applications; development of the ability to understand and apply in the research and applied activities of the modern mathematical apparatus; development of logical, heuristic and algorithmic thinking.

To master the discipline, competencies formed in the study of school mathematics course are necessary. The discipline is closely related to such disciplines as "Complex analysis", "Applied Functional Analysis", "Differential Geometry", "Differential Equations", "Probability Theory and Mathematical Statistics", "Optimization Methods", "Equations with Partial Derivatives".

3. The content of the working program (the volume of the discipline, types and types of classes, educational and methodological support of independent work of students)

The content of the working program is presented in Appendix № 1.

4. Evaluation funds for the discipline

4.1. List of competencies and indicators of achievement of competencies with the planned learning outcomes related to them in the discipline. Description of criteria and scales for evaluating the results of training in the discipline.

Code and definition of each competence.

GPC-1: Ability of applying the fundamental knowledge gained in the field of mathematical and (or) natural sciences and using them in professional activities.

Level of competence acquirement	Planned learning outcomes (indicators of achievement of a predetermined level of acquired competencies)	Evaluation criteria for the results			
		2 (" Non-satisfactory")	3 ("Satisfactory")	4 ("Good")	5 ("Excellent")
First level	To know: basic concepts of disciplines, basic theorems and their consequences, methods of solving and analyzing typical problems	Lack of knowledge	Incomplete ideas about the basic concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems	Formed knowledge and skills, but containing separate gaps in the basic concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems	Formed systematic knowledge and skills on the basic concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems

Second level	Be able to: use the knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution	Lack of skills	Partial skills of using the knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution	Generally formed skills, but containing some gaps in the ability of using knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution	Well-formed ability using the knowledge of the disciplines in practice, correctly formulate specific tasks and reasonably choose methods of their solution
Third level	Be in possession of: basic mathematical knowledge and its application for solving theoretical and applied problems	Lack of formed skills	Generally successful, but non-systematic application of basic mathematical knowledge for solving theoretical and applied problems	Generally successful, but containing some gaps in the application of basic mathematical knowledge for solving theoretical and applied problems	Successful acquisition of basic mathematical knowledge and its application for solving theoretical and applied problems

Evaluation criteria are the points which are given by the teacher to each student for different types of activities (evaluation tools) at the end of the study of each module (section of a discipline) that are listed in the rating plan of the discipline (for the exam: current control –40 points maximum; periodical control – 30 points maximum, bonus points – 10 points maximum. For the grade of “pass”: current control - 50 points maximum; periodical control – 50 points maximum, bonus points – 10 points maximum).

Grading scale:

(for the exam:

45 to 59 points – "satisfactory";

60 to 79 points – "good";

80 points – "excellent".

for the grade of “pass”:

“passed” - **from 60 to 110** rating points (including 10 bonus points),

“failed” - **from 0 to 59** rating points).

4.2. Standard control tasks or other materials necessary for evaluating the results of training in the discipline, correlated with

Level of competence acquirement	Planned learning outcomes (indicators of achievement of a predetermined level of acquired competencies)	Evaluation criteria for the results (pass/fail rating)	
		Grade of "non pass" ("failed")	Grade of "pass" ("passed")
First level	To know: basic concepts of the disciplines, basic theorems and their consequences, methods of solving and analyzing typical problems	Incomplete ideas about the basic concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems	Well-formed systematic ideas about the main concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems
Second level	Be able to: use the knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution	Partial skills of using the knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution	Well-formed ability of using the knowledge of the disciplines in practice, correctly formulate tasks and reasonably choose methods of their solution
Third level	Be in possession of: basic mathematical knowledge and its application for solving theoretical and applied problems	Generally successful, but non systematic application of basic mathematical knowledge for solving theoretical and applied problems	Successful acquirement of basic mathematical knowledge and its application for solving theoretical and applied problems

the indicators of competence achievement established in the educational program. Methodological materials defining the procedures for evaluating the results of training in the discipline

Indicator of the achieved competence	Results of training in the discipline	Evaluation tools
GPC-1. 1. Possesses basic knowledge gained in the field of mathematical analysis	To know: the basic concepts of the discipline, the main theorems and their consequences, methods of solving and analyzing typical problems	Theoretical survey, exam
GPC-1. 2. Knows how to use them in professional activities	Be able to: use the knowledge of the discipline in practice, correctly formulate tasks and reasonably choose methods of their solution	Laboratory work, test work, pass/fail rating

GPC-1.3. Possesses the skills to choose methods of solving problems in professional activity based on theoretical knowledge.	To possess: basic mathematical knowledge and its application for solving theoretical and applied problems	Laboratory work, test work, pass/fail rating
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Examination tickets

Exam and credit is an assessment tool for all stages of mastering the competencies.

Questions for the exam (first semester):

1. Numerical sets. The method of mathematical induction. Actions on rational numbers. Properties. Irrationality.
2. Scheme for constructing a set of real numbers. Infinite decimal fractions (idf).
3. Comparison of idf. Approximation of real numbers by rational numbers.
4. Facets of number sets. Principles of upper and lower edges of a number set.
5. The limit of a sequence. Properties of the limit.
6. Arithmetical operations on sequences.
7. Limits of a monotone sequence.
8. The lemma of imbedding segments.
9. Lemma on finite coverage.
10. The concept of a subsequence. The lemma for distinguishing a convergent subsequence.
11. The notion of a function. Elementary functions.
12. Two definitions of limit functions in the language of " δ - ε " and in the language of sequences (reduction to the case of a sequence).
13. The first remarkable limit.
14. The second remarkable limit.
15. Arithmetic operations on limits. Limit transition in inequalities.
16. Limit of a monotone function.
17. Comparison of functions. O-symbols. Criterion for equivalence of functions.
18. Continuity of function. 3 definitions. Classification of points of discontinuity. Examples. Arithmetic properties of continuity.
19. Continuity of elementary functions.
20. Properties of continuous functions (Theorems: about constancy of sign, Cauchy about passing through zero, Cauchy about intermediate value).
21. Weierstrass's first and second theorems.
22. Reversibility of a continuous monotone function.
23. Continuity of a complex function.
24. Uniform continuity. Cantor's theorem.

25. Definition of the derivative of a function. The geometrical meaning of the derivative. Examples of the calculation of derivatives. Table of derivatives of basic elementary functions. Representation for the increment of a function. Unilateral derivatives.
26. The derivative of an inverse function.
27. Rules for calculating derivatives (derivative of the sum, product, and quotient of two functions).
28. The derivative of a composite function.
29. Definition of a differentiable function. The relationship between differentiability and the existence of a derivative function. The differential of a function.
30. Invariance of the form of the first differential.
31. Basic theorems of differential calculus. (Fermat's Lemma, Rolle's Theorem, Lagrange's Theorem, Cauchy's Theorem). Geometrical interpretation of these theorems.
32. Derivatives and higher order differentials.
33. Taylor formula for a polynomial. Calculation of coefficients.
34. Decomposition of an arbitrary function by Taylor's formula. The residual term in the Peano form.
35. L'Hopital's rule. Uncertainty $\left(\frac{0}{0}\right), \left(\frac{\infty}{\infty}\right)$
36. The condition of monotonicity of a function in a given interval. Extremes of a function. Necessary and sufficient conditions for the presence of an extremum.
37. Convex functions. Geometrical interpretation. Conditions for convexity of a function.
38. Points of inflection. Asymptotes. Scheme for plotting the graph of a function by characteristic points.

Questions for the exam (second semester):

1. The concept of the antiderivative function. Properties of the indefinite integral. Integration by the method of replacement of a variable.
2. Indefinite integral. Integration by parts. Integration of expressions containing trigonometric functions.
3. An indefinite integral. Simple fractions and their integration.
4. Decomposition of regular fractions into partial fractions.
5. Integration of expressions of the form $R(x)^m \sqrt{\frac{\alpha x + \beta}{\gamma x + \delta}}$
6. Integrating a binomial differential.
7. The area problem.
8. Definition of a definite integral. A necessary condition for integrability.
9. Definitions of Darboux sums. Their properties.

- 10.The condition for the existence of a definite integral.
- 11.Classes of integrable functions (continuous, monotone and bounded).
- 12.Properties of integrable functions.
- 13.Properties of a definite integral expressed by equations.
- 14.Properties of the definite integral expressed by inequalities.
- 15.The average value theorem. The generalized mean value theorem.
- 16.The definite integral as a function of the upper limit.
- 17.The Newton-Leibniz formula.
- 18.The concept of a curve. The arc length of a curve. Straightenable curves.
Definition of the concept of area of a plane figure. The property of additivity. Area as a limit.
- 20.The class of quadratic figures. Expression of area by an integral.
- 21.Area of a curvilinear sector.
- 22.Definition of the concept of volume. Expression of volume by an integral.
- 23.The area of a surface of rotation.
- 24.Space \mathbb{R}^n . Metric. Norm of an element.
- 25.Open and closed sets in \mathbb{R}^n . Closedness criterion. Compact in \mathbb{R}^n .
- 26.The limit of a function of many variables. Reduction to the case of a sequence. The Bolzano-Weirstrass theorem for the extraction of a convergent subsequence.
- 27.Repeated limits. The relation between double and repeated limits.
- 28.Definition of the continuity of a function of many variables. Basic properties of continuous functions.
- 29.Partial derivatives and partial differentials. The total increment of a function.
- 30.The total differential of a function of many variables.
- 31.The derivatives of a composite function of many variables.
- 32.The derivative in a given direction. Gradient.
- 33.The derivatives of higher orders of a function of many variables. Theorem on mixed derivatives.
- 34.Extremes of functions of many variables. A necessary condition.
- 35.Extremes of functions of many variables. A sufficient condition.
- 36.The concept of numerical series. The sum of an infinite geometrical progression. Prerequisite for the convergence of a series. Cauchy criterion.
- 37.Significant positive series. Sufficient conditions for convergence (boundedness, comparison sign, Dalembert's test).
- 38.Famously positive series. Sufficient conditions for convergence (boundedness, Cauchy's test, Raabe's test, integral test).
- 39.Absolute and conditional convergence of numerical series. Leibniz's test of the convergence of

a sign-convergent series.

40. Arbitrary numerical series. The Abel transformation. Abel's and Dirichlet's tests.

Structure of the examination ticket:

1. Theoretical question.
2. Theoretical question

Grading criteria (in points):

- **25-30 points** if student demonstrates the knowledge of 80% or more of the required educational material in the discipline.

- **17-24 points** if student demonstrates the knowledge from 60% to 79% of the required educational material in the discipline.

- **10-16 points** if student demonstrates the knowledge from 45% to 59% of the required educational material in the discipline.

- **1-10 points** if student demonstrates the knowledge less than 45% of the required educational material in the discipline.

An example of examination tickets is given in Appendix 2.

Sample questions for verbal examination (Semester 1)

Module 1.

1. Irrationality .
2. Infinite decimals.
3. The method of mathematical induction.
4. Properties of natural numbers.
5. Properties of integers.
6. Properties of rational numbers.
7. The principle of the upper (lower) bound of a number set.
8. The limit of a sequence.

Module 2.

1. The limit of a function.
2. The first remarkable limit.
3. The second remarkable limit.
4. The number e .
5. The limit transition in equality and inequality.
6. Continuity of a function at a point.
7. Continuity of elementary functions.

Module 3.

- 1.. Properties of continuous functions.
- 2.. Uniform Continuity.
3. The derivative of a function of one variable. Geometrical meaning.
4. Derivatives of elementary functions.
5. The derivative of the sum, product, and quotient of two functions.
6. The derivative of a complex function.

Module 4.

1. The invariance of the form of the first differential.
2. Basic theorems of differential calculus.
3. Taylor's formula.
4. L'opital's rule.
5. Extremes of functions of one variable.

Sample questions for verbal examination (Semester 2)

Module 1..

1. Definition of the antiderivative function.
2. Properties of an indefinite integral.
3. Substitution of a variable in an indefinite integral.
4. Integration by parts.

Module 2..

1. The definite integral.
2. The necessary condition for integrability.
3. The upper and lower sums of Darboux.
4. The condition for the existence of a definite integral.
5. The average value theorem.

6. The Newton-Leibniz formula.
7. Calculation of arc length.
8. The area of a curvilinear sector.

Module 3.

1. A necessary condition for the convergence of a numerical series.
2. The Cauchy criterion.
3. Cauchy's test.
4. The test of comparison.
5. Leibniz's test.
6. Absolute and conditional convergence of numerical series.
7. Abel's and Dirichlet's tests.

Each student is given one question from each module during the semester.

Each question is graded 2 points. These points are taken into account when calculating the rating only for the exam.

Grading criteria (in points):

- 15 points are awarded to a student if he/she gives a clear, detailed and correct answer to the question;

- 10-14 points are awarded if the student gave a correct answer, but may be incomplete or did not answer 1-2 additional questions;

- 1-9 points are awarded if the student gave an incorrect answer to the question, but answered additional questions or gave a fragmented, but correct answer to the main question, but did not answer additional questions;

- 0 points will be assigned to the student if he or she fails to answer the main question and does not answer any additional questions.

Work in class

Class work: solving problems from the book [3]. Each activity is graded 1 point.

Assignments for laboratory work

Each lab work consists of several problems on the topic being tested. Each student is given a separate version. All laboratory works are performed by each student independently. The problem is considered solved correctly if the correct solution is written in detail and clearly. Upon completion of the laboratory work, the student submits a report that contains the solutions to the problems on the given laboratory work.

Examples of a variant of the laboratory work:

1. Proof $1^3 - 2^3 + 3^3 - 4^3 + \dots + (2n - 1)^3 - (2n)^3 = -n^2(4n + 3)$.
2. Find limits a) $\lim_{n \rightarrow \infty} \frac{(2n+1)^2 - (n+1)^2}{n^2 + n + 1}$; b) $\lim_{n \rightarrow \infty} \frac{n^3 \sqrt{3n^2 + 4} \sqrt{4n^8 + 1}}{(n + \sqrt{n}) \sqrt{7 - n + n^2}}$; c) $\lim_{n \rightarrow \infty} \left(\frac{n+2}{n-1}\right)^n$;
- d) $\lim_{n \rightarrow 0} \frac{n^3 - n^2 + 2n}{n^2 + n}$; e) $\lim_{n \rightarrow 3} \frac{n^2 + n - 12}{\sqrt{n-2} - \sqrt{4-n}}$.
3. Check if the sequence converges $x_n = \frac{\sqrt[5]{n^3} \cos n!}{n+2}$.
4. $x_n = -1 + 3(-1)^{n+1}$. Find $\inf x_n, \sup x_n$.

5. $x_n = (-1)^{n+1}n$. Find $\lim_{n \rightarrow \infty} x_n$, $\overline{\lim}_{n \rightarrow \infty} x_n$.

Description of the evaluation methodology for the tests:

Grading Criteria (in points): The maximum number of points a student can earn for a correctly solved problem is written in front of each problem. For solving the problem you can get 0.5, 1, 1.5, 2 or 3 points depending on the correctness of the solution given (there can be inaccuracies in the solution, incomplete solution, not completely correct solution).

Examples of a variant of the test:

1. Proof $\lim_{n \rightarrow \infty} \frac{2n^4+1}{2n^4+n^3} = 1$ (3 points)
2. Define a sequence that converges to $+\infty$. (1 points)
3. Proof $1 \cdot 2 \cdot 3 + 2 \cdot 3 \cdot 4 + 3 \cdot 4 \cdot 5 + \dots + n(n+1)(n+2) = \frac{n(n+1)(n+2)(n+3)}{4}$. (3 points)

Exemplary topics for course papers

Investigate the function $f(x) = \dots$

Algorithm

1. Find the area of definition. Identify singular points (points of discontinuity).
2. Check for vertical asymptotes at the points of discontinuity and on the boundaries of the definition.
3. Find the points of intersection with the axes of coordinates.
4. Determine whether the function is even or odd.
5. Determine if the function is periodic or not (only for trigonometric functions).
6. Find points of extremum and intervals of monotonicity.
7. Find inflection points and convex-concave intervals (if possible).
8. Investigate the behavior at infinity. Find inclined asymptotes.
9. Select additional points and calculate their coordinates.
10. Plot the graph and asymptotes.
11. Calculate the integral on the interval $[a; b]$ using the trapezium method.
12. Check your results in any program (Maple, Alpha Wolfram etc.).

4.3. Rating – plan of the discipline

Rating-plan of the discipline is given in Appendix 3.

5. Educational, methodic and informational support of the discipline.

5.1. List of references to primary and complementary educational literature necessary for acquiring the discipline.

Primary literature

1. Fichtenholz G.M. Course of differential and integral calculus. In 3 vols. M.: Fizmatlit, 2001. (in Russian) http://biblioclub.ru/index.php?page=book_red&id=83037
2. William F. Trench Introduction to Real Analysis <https://digitalcommons.trinity.edu/mono/7/>
3. Demidovich B.P. Collection of Problems and Exercises in Mathematical Analysis: Textbook for Universities Moscow: CheRo, 1997. http://biblioclub.ru/index.php?page=book_red&id=459722

Auxiliary literature:

4. Никольский С.М. Курс математического анализа. Т.1, М.: Физматлит, 2001. http://biblioclub.ru/index.php?page=book_red&id=69500
5. Ильин В.А., Позняк Э.Г. Основы математического анализа в 2-х частях. М.: Физматлит, 2009. http://biblioclub.ru/index.php?page=book_red&id=83225
6. Амангильдин Т.Г., Ахмерова Э.Ф. Производная и ее приложения к решению задач: метод. указания и задания с решениями типовых задач по математическому анализу– Уфа: РИЦ БашГУ, 2013. <https://elib.bashedu.ru/dl/corp/AmangildinProizvodPrilozhRashZadach.pdf/info>
7. Рудин У. Основы математического анализа. – М.: Мир, 1976. http://biblioclub.ru/index.php?page=book_red&id=447958
8. Б. Гелбаум, Дж. Олмстед. Контрпримеры в анализе. – М.: Мир, 1967. http://biblioclub.ru/index.php?page=book_red&id=459728
9. Г. Полия, Г. Сеге. Задачи и теоремы из анализа. Ч.1, - М.: Наука. 1978. http://biblioclub.ru/index.php?page=book_red&id=447989
10. Мараховский А.С., Белаш А.Н. Математический анализ: интегральное исчисление: практикум. Ставрополь: СКФУ, 2015. http://biblioclub.ru/index.php?page=book_red&id=458071
11. Туганбаев А.А. Математический анализ: производные и графики функций. Учебное пособие. М.: Изд-во «Флинта», 2017. http://biblioclub.ru/index.php?page=book_red&id=103836
12. Туганбаев А.А. Математический анализ: ряды. Учебное пособие. М.: Изд-во «Флинта», 2017. http://biblioclub.ru/index.php?page=book_red&id=103837
13. Туганбаев А.А. Математический анализ: интегралы. Учебное пособие. М.: Изд-во «Флинта», 2017. http://biblioclub.ru/index.php?page=book_red&id=103835
14. Протасов Ю.М. Математический анализ. Учебное пособие. М.: Изд-во «Флинта», 2012. http://biblioclub.ru/index.php?page=book_red&id=115118

5.2. List of the Internet resources and software necessary for acquiring the discipline, including professional data bases and reference systems.

1. Library of Bashkir State University <http://lib.bashedu.ru>
2. BashSU Electronic Library System <https://elib.bashedu.ru>
3. University WebWork server: <http://webwork-okko.bashedu.ru/webwork2/>.

**6. Hardware equipment, materials and rooms necessary for implementing the educational process
in the discipline.**

<i>Names of specialized rooms, rooms and laboratories</i>	<i>Activity form</i>	<i>Name of the equipment/software</i>
<i>1</i>	<i>2</i>	<i>3</i>
Rooms 501,517, 528 or any other room according to the current time table	<i>Lectures</i>	The board for writing, projector and screen
Rooms 517, 503 or any other room according to the current time table	<i>Laboratory</i>	The board for writing, projector and screen
Library, reading halls	<i>Individual work</i>	Internet. The university WebWork server

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CONTENT OF THE WORKING PROGRAM

of the discipline Analysis I for semester 1

Activity	Duration
Total duration of the discipline (CUD / hours)	7/252
Academic hours for the work with instructor	
lectures	54
laboratory	72
other (consultation in group or individually and other forms of learning activities assuming collaboration of learners with instructor)	1,7
Academic hours for individual work of learners	71,5
Academic hours for preparing to exam/credit test/differentiated credit test (Grading)	52,8
laboratory	

Final grading:
exam in semester 1

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CONTENT OF THE WORKING PROGRAM

of the discipline Analysis I for semester 2

Activity	Duration
Total duration of the discipline (CUD / hours)	6/216
Academic hours for the work with instructor	
lectures	48
laboratory	64
other (consultation in group or individually and other forms of learning activities assuming collaboration of learners with instructor)	1,7
Academic hours for individual work of learners	58,5
Academic hours for preparing to exam/credit test/differentiated credit test (Grading)	43,8
laboratory	

Final grading:
exam in semester 2

Semester 1

Item no.	Topic and its content	Learning forms: lectures, seminars, laboratory, and individual work with duration (in academic hours)				Primary and auxiliary literature (numbers in the reference list)	Task for individual work of learners	Forms of current grading (colloquia, quizzes, computer tests etc)
		LEC	SEM	LAB	IND			
1	2	3	4	5	6	7	8	9
1.	The subject of mathematical analysis, information about sets and logical symbolism, mapping and functions.	2	-	2	4	1-3,	[3]: 22-29, 151-154	Theoretical survey
2.	Real numbers: algebraic properties of the set \mathbb{R} of real numbers. Infinite decimal fractions.	3	-	4	4	1-3	[3]: 3, 4, 6, 10,	Theoretical survey
3.	The axiom of set completeness \mathbb{R} . Basic principles of completeness of the set \mathbb{R} : existence of exact upper (lower) bound of the numerical set, principle of nested segments, the lemma of finite coverage.	3	-	2	4	1-3	[3]: 16, 17, 20, 21	Laboratory work No.1
4.	Limit theory: the limit of a numerical sequence; basic properties and signs of the existence of limit.	2	-	6	4	1-3	[3]: 48, 52, 57, 60, 63	Laboratory work No.1

5.	Limit points of a set and Bolzano-Weierstrass theorem for the separation of a convergent subsequence; the limit of a monotone sequence.	3	-	2	4	1-3	[3]: 69,79, 101, 104-109	Laboratory work No.1
6.	Number "e", upper and lower limits; Cauchy criterion for the existence of limit.	3	-	2	4	1-3	[3]: 84, 85, 74, 72, 111-114	Theoretical survey
7.	The limit of a function at a point. Various definitions and their equivalences. The Cauchy criterion for the existence limit.	3	-	6	4	1-3	[3]: 406, 407	Laboratory work No.2
8.	Properties of limits. Arithmetic operations on limits. The 1st and 2nd remarkable limits.	3	-	4	4	1-3	[3]:70,72,74,76,145-147	Laboratory work No.2
9.	Classification of infinitesimal and infinitely large. Symbols "O", "o".	4	-	4	4	1-3	[3]: 647-651	Laboratory work No.2
10.	Continuous functions: local properties of Continuous functions; Continuity of a function from a function; point of discontinuity; Boundedness of a function that is continuous on a segment.	4	-	6	4	1-3	[3]: 674-728	Laboratory work No.2, Theoretical survey
11.	Existence of maximum and minimum values; Uniform continuity of a function that is continuous on the segment.	4	-	4	4	1-3	[3]: 794-801	Laboratory work No.2
12.	Monotone functions, existence and continuity of inverse function, continuity of elementary functions.	4	-	4	4,8	1-3	[3]: 767-772	Theoretical survey

13.	Differentials and Derivatives: The differentiability of a function at a point; the derivative at a point, the differential and their geometric meaning; the mechanical meaning of the derivative; the rules of differentiation; derivatives and differentials of higher orders; the Leibniz's formula.	4	-	6	5	1-3	[3]: 828, 845-859, 888-892, 920-932, 961-966, 1039-1042, 1055-1063, 1085-1090, 1099, 1134-1141	Laboratory work No.3
14.	Basic theorems of differential Rolle's, Lagrange's and Cauchy's theorems on finite increments. Basic theorems of differential Local Taylor formula; asymptotic expansions of elementary functions; Taylor formula with residual term.	4	-	6	5	1-3	[3]: 1251, 1377-1387	Theoretical survey
15.	Application Differential The application of differential calculus to the study of functions. Signs of constancy, monotonicity, extremes, convexity, inflection points.	4	-	10	8	1-3	[3]: 1479-1498	Laboratory work No.3
16.	Lopital's rule	4		4	5	1-3	[3]: 1345-1364	Laboratory work No.3

Semester 2

Item no.	Topic and its content	Learning forms: lectures, seminars, laboratory, and individual work with duration (in academic hours)				Primary and auxiliary literature (numbers in the reference list)	Task for individual work of learners	Forms of current grading (colloquia, quizzes, computer tests etc)
		LEC	SEM	LAB	IND			
1	2	3	4	5	6	7	8	9
1.	The original. The indefinite integral and its properties. Table of formulas for integration. Substitution of a variable. Integration by parts.	6		8	8	1-3	[3]: 1628-1632, 1643-1660	Theoretical survey
2.	Integration of rational functions and Irrational functions.	6		8	8	1-3	[3]: 1870-1887, 1929-1935, 1939-1947, 1955, 1957	Verbal questioning
3.	The definite integral: Problems leading to the concept of the definite integral. The definite integral Riemann; the criterion of integrability; integrability of a continuous function, monotone function and bounded function with a finite number of points	6	-	8	8	1-3	[3]: 2210-2213, 2220-2223, 2242-2248	Laboratory work No.1, verbal questioning

4.	Properties of the definite integral. The average value theorem. Differentiation by a variable upper limit. The existence of a first form from a continuous of a function. Relation of the definite integral to the indefinite: Nyton-Leibniz formula. Substitution of a variable; integration by parts; arc length and other Geometrical, mechanical and physical applications.	6	-	8	8	1-3	[3]: 2398-2406, 2413-2415,2418-2421,2436,2440,2447, 2474 -2476,2493-2498	Laboratory work No.1, verbal questioning
5.	Functions of Many Variables: Euclidean Space. An overview of the basic metric and topological characteristics of point sets of Euclidean space. Limits, continuity of a function of many variables.	8	-	10	10	1-3	[3]: 3184-3192	Laboratory work No.3, verbal questioning
6.	Differential and partial derivatives of a function of many variables. Directional derivatives, gradient. Sufficient condition of differentiability; tangent and normal to surface.	6	-	8	8	1-3	[3]: 3214-3228, 3245, 3269-3271, 3283, 3284, 3293-3297	Laboratory work No.3

8.	Numerical series: convergence and sum of numerical series; Cauchy criterion; familiar-constant series; comparison of series; Cauchy's convergence; Cauchy's integral criterion of convergence. convergence.	5	-	8	4	1-3	[3]: 2548-2551, 2580-2582, 2626-2635	Laboratory work No.4
9.	Leibniz's test; absolute and conditional convergence; Abel transformation and its application to series; permutation of Absolute Convergent Series; Riemann's Theorem; operations on series; double series; concept of infinite products.	5	-	6	4,5	1-3	[3]: 2667-2670, 2675-2689	Laboratory work No.5, verbal questioning
	Course papers		-			1-3	A properly formatted study paper with elements of independent research on a proposed topic, accompanied by appropriate examples and graphs that illustrate the theoretical material studied.	
	Всего часов:	48		64	58,5			

An example of examination tickets (semester 1)

FEDERAL STATE BUDGETARY EDUCATIONAL INSTITUTION
OF HIGHER EDUCATION
«BASHKIR STATE UNIVERSITY»
FACULTY OF MATHEMATICS AND INFORMATION TECHNOLOGIES
Department of Mathematical Analysis

**EXAMINATION TICKET #1
on “Analysis I”**

1. Numerical sets. The method of mathematical induction. Actions on rational numbers. Properties. Irrationality.
2. L’opital’s rule. Uncertainty $\left(\frac{0}{0}\right), \left(\frac{\infty}{\infty}\right)$

An example of examination tickets (semester 2)

FEDERAL STATE BUDGETARY EDUCATIONAL INSTITUTION
OF HIGHER EDUCATION
«BASHKIR STATE UNIVERSITY»
FACULTY OF MATHEMATICS AND INFORMATION TECHNOLOGIES
Department of Mathematical Analysis

**EXAMINATION TICKET #2
on “Analysis I”**

1. An indefinite integral. Simple fractions and their integration.
2. The derivative in a given direction. Gradient.

Rating – plan of the discipline

Analysis I

(the name of the discipline according to the working curriculum)

Direction 01.03.02 Applied Mathematics and Informatics

Grade 1, semester 1

Rating-plan No. 1 (exam)

Types of educational activities of students	Points for a specific task	Number of tasks per semester	Points	
			minimum	maximum
Module 1. The limit of the sequence.				
Current control			0	10
Classroom work	1	10	0	10
Periodical control			0	7,5
Theoretical survey (inquiry)	2,5	3	0	7,5
Module 2. The limit of the function. Continuity.				
Current control			0	10
Classroom work	1	10	0	10
Periodical control			0	7,5
Theoretical survey (inquiry)	2,5	3	0	7,5
Module 3. Differentiability of the function.				
Current control			0	10
Classroom work	1	10	0	10
Periodical control			0	7,5
Theoretical survey (inquiry)	2,5	3	0	7,5
Module 4. Research of function				
Текущий контроль Current control			0	10
Работа на занятии Classroom work	1	10	0	10
Рубежный контроль Periodical control			0	7,5
Theoretical survey Theoretical survey (inquiry)	2,5	3	0	7,5
Bonus points				
1. Student academic competition or essay contest			0	5
2. Volunteering assistance in administrating of student academic competition or essay contest			0	5
Attendance (points are deducted from the total amount of points scored)				
1. Attending lectures			0	-6
2. Attending practical classroom work (seminar, laboratory classes)			0	-10
Final control				
Exam			0	30
Total points			45	100

Rating – plan of the discipline

Analysis I

(the name of the discipline according to the working curriculum)

Direction 01.03.02 Applied Mathematics and Informatics

Grade 1, semester 2

Rating-plan No. 2 (exam)

Types of educational activities of students	Points for a specific task	Number of tasks per semester	Points	
			minimum	maximum
Module 1. Antiderivative function				
Current control			0	10
Classroom work	1	10	0	10
Periodical control			0	10
Theoretical survey (inquiry)	2,5	4	0	10
Module 2. Definite Integral				
Current control			0	15
Classroom work	1	15	0	15
Periodical control			0	10
Theoretical survey (inquiry)	2,5	4	0	10
Module 3. Numerical series				
Current control			0	15
Classroom work	1	15	0	15
Periodical control			0	10
Theoretical survey (inquiry)	2,5	4	0	10
Bonus points				
1. Student academic competition or essay contest			0	5
2. Volunteering assistance in administrating of student academic competition or essay contest			0	5
Attendance (points are deducted from the total amount of points scored)				
1. Attending lectures			0	-6
2. Attending practical classroom work (seminar, laboratory classes)			0	-10
Final control				
Exam			0	30
Total points			45	100